

IN THE UNITED STATES PATENT AND TRADEMARK OFFICE

Patent Number: 7,277,832
Issued: October 2, 2007
Name of Patentee: Hsiao-Dong Chiang
Title of Invention: "Dynamical Method for Obtaining Global Optimal Solution
of General Nonlinear Programming Problems"

**Commissioner of Patents
Attn: Certificate of Correction Branch
P. O. Box 1450
Alexandria, VA 22313-1450**

**REQUEST FOR CERTIFICATE OF CORRECTION OF PATENT
FOR PTO MISTAKE (37 CFR 1.322)**

1. Attached in duplicate is Form PTO-1050 with at least one copy being suitable for printing.
2. The exact page and line number where errors occur in the issued patent are:

Claim 2, Column 24, line 53: Delete " x_5 " and add -- x_s --.

Claim 5, Column 25, line 22: Delete the word "to" and add -- t_0 --.

Claim 7, Column 25, line 63: Delete the word "to" and add -- t_0 --.

Claim 14, Column 28, line 46: Delete " $x_{s,j}^{0}$ " and add the figure -- $x_{s,0}^{j+1}$ --.

Attached is a copy of the Amendment After Final filed April 3, 2007, showing the correct wording of the claims. Please note that claim 2 in the issued patent is equivalent to claim 16 in the amendment. Claim 5 in the issued patent is equivalent to claim 19 in the amendment. Claim 7 in the issued patent is equivalent to claim 21 in the amendment and claim 14 in the issued patent is equivalent to claim 38 in the amendment.

4. Please send the Certificate to:

Lynda M Wood
Brown & Michaels, P.C.
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By: _____/Lynda Wood, Reg. #53791/
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UNITED STATES PATENT AND TRADEMARK OFFICE

CERTIFICATE OF CORRECTION

PATENT NO. : 7,277,832
DATED: October 2, 2007
INVENTOR(S): Hsiao-Dong Chiang

It is certified that error appears in the above-identified patent and that said Letters Patent is hereby corrected as shown below:

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MAILING ADDRESS OF SENDER:

PATENT NO. 7,277,832

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(PTO FORM 1050)

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IN THE UNITED STATES PATENT AND TRADEMARK OFFICE

April 3, 2007

Serial No. 09/849,213
Applicant: Hsiao-Dong Chiang
Filed: May 4, 2001
Title: Dynamical Method for Obtaining Global Optimal Solution of General Nonlinear Programming
Art Unit: 2128
Examiner: Thai Q. Phan
Confirmation Number: 9034
Attorney Docket No.: CIG-1

HONORABLE COMMISSIONER OF PATENTS
Alexandria, VA 22313-1450

AMENDMENT AFTER ALLOWANCE

In response to the telephone call from Examiner Phan on April 3, 2007, , please amend the above-identified application as follows:


Amendments to the Claims are reflected in the listing of claims which begins on page 2 of this paper.

Remarks/Arguments begin on page 18 of this paper.

Certificate of Facsimile Transmission

I hereby certify that this correspondence is being facsimile transmitted to the Patent and Trademark Office (Fax No. (571) 273-3783) on April 3, 2007, at 11:45AM

Signature


Michael F. Brown, Reg. No. 29,619

Amendments of the Claims:

A detailed listing of all claims in the application is presented below. This listing of claims will replace all prior versions, and listings, of claims in the application. All claims being currently amended are submitted with markings to indicate the changes that have been made relative to immediate prior version of the claims. The changes in any amended claim are being shown by strikethrough (for deleted matter) or underlined (for added matter).

Claims 1-14. (Canceled)

15. (Currently Amended) A practical numerical computer-implemented method for reliably computing a dynamical decomposition point of a stable equilibrium point for large-scale nonlinear systems, comprising the steps of:

- a) given a stable equilibrium point x_s ;
- b) moving along a search path $\phi_t(x_s) \equiv \{x_s + t \times \hat{s}, t \in \mathbb{R}^+\}$ starting from x_s and detecting an exit point, x_{ex} , at which said search path $\phi_t(x_s)$ exits a stability boundary of a stable equilibrium point x_s ;
- c) using said exit point x_{ex} as an initial condition and integrating a nonlinear system (4.2) to an equilibrium point x_d ; and
- d) computing said dynamical decomposition point with respect to the stable equilibrium point x_s wherein said search path is x_d ; and
- e) displaying the dynamical decomposition point.

16. (Currently Amended) The method of claim 15, wherein a method for computing said exit point of the nonlinear system (4.3) comprises the step of moving along said search path $\phi_t(x_s) \equiv \{x_s + t \times \hat{s}, t \in \mathbb{R}^+\}$ starting from x_s and detecting said exit point x_{ex} , which is a first local maximum of an objective function $C(x)$ along said search path $\phi_t(x_s)$.

17. (Currently Amended) The method of claim 15, wherein a method for computing a dynamical decomposition point comprises the steps of:

- a) using said exit point x_{ex} as an initial condition and integrating a nonlinear system (4.2) to a first local minimum of a norm $\|F(x)\|$ along the corresponding trajectory, where $F(x)$ is a vector field of the nonlinear system (4.2), and letting the point at which the first local minimum of $\|F(x)\|$ occurs be denoted x_d^0 , and is called the minimum distance point (MDP); and
- b) using said MDP x_d^0 as an initial guess and solving a set of nonlinear algebraic equations of said vector field (4.2) $F(x) = 0$, wherein a solution is x_d , and a dynamical decomposition point with respect to the local optimal solution x_s and said search path $\phi_t(x_s)$ is x_d .

18. (Currently Amended) The method of claim 15, wherein a method for computing said exit point with respect to a stable equilibrium point of the nonlinear system (4.2) and a search vector comprises the step of computing an inner-product of said search vector and the vector field of the nonlinear system (4.3) at each time step, by moving along said search path $\phi_t(x_s) \equiv \{x_s + t \times \hat{s}, t \in \mathbb{R}^+\}$ starting from x_s and at each time-step, computing an inner-product of said search vector \hat{s} and vector field $F(x)$, such that when a sign of said inner-product changes from positive to negative, said exit point is detected.

19. (Currently Amended) The method of claim 15, wherein a method for computing said exit point of the nonlinear system (4.3) with respect to a stable equilibrium point and a search vector comprises the steps of:

- a) moving from said stable equilibrium point along said search vector until an inner-product of said search vector and the vector field of the nonlinear system (4.3) changes sign between an interval $[t_1, t_2]$;

- b) applying a linear interpolation to an interval $[t_1, t_2]$, which produces an intermediate time t_0 where an interpolated inner-product is expected to be zero;
- c) computing an exact inner-product at t_0 , such that if said value is smaller than a threshold value, said exit point is obtained; and
- d) if said inner-product is positive, then replacing t_1 with t_0 , and otherwise replacing t_2 with t_0 and going to step b).

20. (Currently Amended) The method of claim 15, wherein a method for computing a minimum distance point (MDP) of the nonlinear system (4.2) satisfying required conditions (C1) and (C2) comprises the steps of:

- a) using said exit point as an initial condition and integrating the nonlinear system (4.2) for a few time-steps, and letting the end point be denoted as the current exit point;
- b) checking convergence criterion, and, if a norm of said current exit point obtained in step a) is smaller than a threshold value, then declaring said point as said MDP and stopping the process, otherwise, going to step c); and
- c) drawing a ray connecting a current exit point on a trajectory and a local optimal solution (equivalently, a stable equilibrium point), replacing said current exit point with a corrected exit point, which is a first local maximal point of objective function along said ray, starting from the stable equilibrium point, and assigning this point to said exit point and going to step a).

21. (Currently Amended) The method of claim 15, wherein a method for computing said dynamical decomposition point of the nonlinear system (4.2) satisfying required conditions (C1) and (C2) with respect to a stable equilibrium point x_* and a search vector \hat{s} , comprises the steps of:

- a) moving along said search path $\varphi_t(x_s) \equiv \{x_s + t \times \hat{s}, t \in \mathbb{R}^+\}$ starting from x_s and detecting a moment that an inner-product of said search vector \hat{s} and the vector field $F(x)$ of the nonlinear system (4.2) changes sign, between an interval $[t_1, t_2]$, stopping this step if t_1 is greater than a threshold value and reporting that there is no adjacent local optimal solution along this search path, otherwise, going to step b);
- b) applying linear interpolation to said interval $[t_1, t_2]$, which produces an intermediate time t_0 where said interpolated inner-product is expected to be zero, computing an exact inner-product at t_0 , and if said value is smaller than a threshold value, said exit point is obtained, and going to step d);
- c) if said inner-product is positive, then replacing t_1 with t_0 , and otherwise replacing t_2 with t_0 and going to step b);
- d) using said exit point as an initial condition and integrating a the nonlinear system (4.2) for a few time-steps, and letting the end point be denoted as the current exit point;
- e) checking convergence criterion, and if a norm of said point obtained in step d) is smaller than a threshold value, then declaring said point as the MDP and going to step g), otherwise going to step e);
- f) drawing a ray connecting a current exit point on said trajectory and a stable equilibrium point, replacing said current exit point with a corrected exit point which is a first local maximal point of objective function along said ray starting from the stable equilibrium point, and assigning this point to said exit point and going to step d); and
- g) using said MDP as an initial guess and solving a set of nonlinear algebraic equations of the vector field of the nonlinear system (4.2) $F(x) = 0$,

wherein a solution is t_d , such that said DDP with respect to a stable equilibrium point x_s and search vector \hat{s} is x_d .

22. (Cancelled)

23. (Currently Amended) A hybrid search computer-implemented method for obtaining a local optimal solution of a general unconstrained nonlinear programming problem (4.1) starting from any initial point, comprising the steps of:

- a) given an initial point x_0 ;
- b) integrating a nonlinear dynamical system ~~described by (4.2)~~ that satisfies required conditions ~~(C1) and (C2)~~ from said initial point x_0 to obtain a trajectory $\phi_i(x_0)$ for n time-steps, n being an integer, and recording the last time-step point as the end point, and if it converges to a local optimal solution, then stopping, otherwise, going to step (c);
- c) monitoring a desired convergence performance criterion along the trajectory $\phi_i(x_0)$ in terms of the rate of decreasing values in the objective function under study, and if the desired criterion is satisfied, then using the end point of trajectory $\phi_i(x_0)$ as the initial point and going to step (b), otherwise, going to step (d); and
- d) applying an effective local optimizer (*i.e.*, a method to find a local optimal solution) from said end point in step (b) to continue the search process, and if it finds a local optimal solution, then displaying the local optimal solution and stopping, otherwise, setting the end point of trajectory $\phi_i(x_0)$ as the initial point, namely x_0 , and going to step (b).

24. (Cancelled)

25. (Previously Presented) The method of claim 14-23, wherein in step (a) the initial point x_0 is given by a method comprising the steps of:

- a) moving along a search path starting from a local optimal solution x_{opt} and applying a DDP search method to compute a corresponding DDP, and if a DDP can be found, then going to step (b), otherwise, trying another search path and repeating this step;
- b) letting said DDP be denoted as x_d , and if x_d has previously been found, then going to step a), otherwise going to step c); and
- c) setting $x_o = x_{opt} + (1 + \varepsilon)(x_d - x_{opt})$ where ε is a small number, and applying a hybrid search method starting from x_o to find a corresponding adjacent local optimal solution.

26. (Previously Presented) A computer-implemented method for obtaining a global optimal solution of unconstrained nonlinear optimization problems, comprising the steps of:

- a) choosing a starting point;
- b) applying the hybrid search method of claim 23 using said starting point to find a local optimal solution x_s^0 ;
- c) setting $j = 0$, $V_s = \{x_s^0\}$, $V_{new}^j = \{x_s^0\}$ and $V_d = \{\emptyset\}$;
- d) wherein set $V_{new}^{j+1} = \{\emptyset\}$ and for each local optimal solution in V_{new}^j (i.e., x_s^j), performing steps (e) through (k);
- e) defining a set of search vectors S_i^j , $i = 1, 2, \dots, m_j$, and setting $i = 1$;
- f) if $i > m_j$, then going to step (l); otherwise, applying a DDP search method along the search vector S_i^j to find a corresponding dynamical

- decomposition point (DDP), and if a DDP is found, then going to step (g), otherwise, setting $i = i + 1$ and going to step (f);
- g) letting the found DDP be denoted as $x_{d,i}^j$, checking whether it belongs to the set V_d , i.e., $x_{d,i}^j \in V_d$?, and if it does, then setting $i = i + 1$ and going to step (f), otherwise setting $V_d = V_d \cup \{x_{d,i}^j\}$ and going to step (h);
- h) for the DDP $x_{d,i}^j$, performing steps (i) through (j) to find a corresponding adjacent local optimal solution;
- i) letting $x_{0,i}^j = x_s^j + (1 + \epsilon)(x_{d,i}^j - x_s^j)$, where ϵ is a small number;
- j) applying said hybrid search method using $x_{0,i}^j$ as the initial condition to find the corresponding local optimal solution, and letting it be denoted as $x_{s,j}^i$;
- k) checking whether $x_{s,j}^i$ has been found before, i.e., $x_{s,j}^i \in V_s$?, and if it has already been found, then setting $i = i + 1$ and going to step (f), otherwise, setting $V_s = V_s \cup \{x_{s,j}^i\}$ and $V_{new}^{j+1} = V_{new}^{j+1} \cup \{x_{s,j}^i\}$ and setting $i = i + 1$ and going to step (f);
- l) examining the set of all newly computed local optimal solutions, V_{new}^{j+1} , and if V_{new}^{j+1} is non-empty, then setting $j = j + 1$ and proceeding to step (d), otherwise proceeding to the next step; and
- m) identifying the global optimal solution from said set of local optimal solutions V_s by comparing their corresponding objective function values in set V_s and;
- n) displaying the global optimal solution.

27. (Cancelled)

28. (Currently Amended) A computer-implemented method for obtaining a global optimal solution of a constrained nonlinear programming problem (4.5), comprising the steps of:

a) Phase I: finding all feasible components of the constrained nonlinear programming problem wherein one effective local method is combined with said dynamical trajectory method, comprising the following steps to find a feasible solution of the constrained optimization problem (4.7):

i) given an initial point x_0 ;

ii) integrating a nonlinear dynamical system ~~described by (4.9)~~ that satisfies required conditions ~~(C1-1)~~ and ~~(C1-2)~~ from said initial point to obtain a trajectory $\phi_i(x_0)$ for n time-steps, n is an integer, and recording the last time-step point as the end point, and if it converges to a feasible solution, then stopping, otherwise, going to step (iii);

iii) monitoring a desired convergence performance criterion in the objective function $\|H(x)\|$, a vector norm of $H(x)$ in ~~(4.7)~~ the constrained optimization problem, and if the desired criterion is satisfied, then using the end point of trajectory $\phi_i(x_0)$ as the initial point and going to step (ii), otherwise, going to step (iv); and

iv) applying an effective method from the said end point in step (b) to continue the search process, and if it finds a feasible solution of (4.7) the constrained optimization problem then stopping, otherwise, setting the end point of trajectory $\phi_i(x_0)$ in step (ii) as the initial point and going to step (ii); and

b) Phase II: finding all local optimal solutions for the constrained nonlinear programming problem in each feasible component;

- c) choosing a global optimal solution for the constrained nonlinear programming problem from the local optimal solutions found in step (b); and
- d) displaying the global optimal solution for the constrained nonlinear programming problem.

29. (Currently Amended) The method of claim 28, comprising the steps of:

- a) approaching a path-connected feasible component of a constrained optimization problem ~~(4.5)~~; and
- b) escaping from said path-connected feasible component and approaching another path-connected feasible component of said constrained optimization problem ~~(4.5)~~.

30. (Currently Amended) The method of claim 28, comprising the steps of:

- a) approaching a stable equilibrium manifold of a nonlinear dynamical system ~~(4.9)~~ satisfying required conditions ~~(C1-1) and (C1-2)~~; and
- b) escaping from said stable equilibrium manifold and approaching another stable equilibrium manifold of said nonlinear dynamical system ~~(4.9)~~ satisfying said conditions ~~(C1-1) and (C1-2)~~.

31. (Currently Amended) The method of claim 28, comprising the steps of:

- a) starting from a point in a feasible component and approaching a local optimal solution located in said feasible component of an optimization problem ~~(4.7)~~; and
- b) escaping from said local optimal solution and approaching another local optimal solution of said feasible component of said optimization problem ~~(4.7)~~.

32. (Currently Amended) The method of claim 28, comprising the steps of:

- a) in a deterministic manner, first finding all stable equilibrium manifolds of a nonlinear dynamical system that satisfies required conditions ~~(C1-1)~~ and ~~(C1-2)~~;
- b) in a deterministic manner, finding all stable equilibrium points of a nonlinear dynamical system that satisfies said conditions ~~(C2-1)~~ and ~~(C2-2)~~; and
- c) then from said stable equilibrium point, finding a global optimal solution.

33. (Currently Amended) The method of claim 32, comprising the steps of:

- a) given a feasible solution of constrained nonlinear programming problem ~~(4.5)~~;
- b) finding a stable equilibrium point of a nonlinear dynamical system ~~(4.10)~~ satisfying required conditions ~~(C2-1)~~ and ~~(C2-2)~~;
- c) moving from said stable equilibrium point to a dynamical decomposition point, in order to escape from a local optimal solution; and
- d) approaching another stable equilibrium point of said nonlinear dynamical system ~~(4.10)~~ satisfying said conditions ~~(C2-1)~~ and ~~(C2-2)~~ in the same path-connected feasible component, via said dynamical decomposition point.

34. -36. (Cancelled)

37. (Currently Amended) A hybrid search method for Phase II of claim 28, comprising the following steps to find a local optimal solution of the constrained optimization problem: ~~(4.7)~~.

- a) given a feasible point x_0 ;
- b) integrating a nonlinear dynamical system ~~described by (4.10)~~ that satisfies required conditions ~~(C2-1)~~ and ~~(C2-2)~~ from said initial point to obtain a trajectory $\phi_i(x_0)$ for n time-steps, n is an integer, and recording the last

time-step point as the end point, and if it converges to a local optimal solution, then stopping, otherwise, going to step (c);

- c) monitoring a desired convergence performance criterion in an objective function $C(x)$ of (4.5), and if the desired criterion is satisfied, then using the end point of trajectory $\phi_t(x_0)$ as the initial point and going to step (b), otherwise, going to step (d); and
- d) applying an effective method from the said end point in step (b) to continue the search process, and if it finds a feasible solution of (4.7) the constrained optimization problem then stopping, otherwise, setting the end point of trajectory $\phi_t(x_0)$ in step (b) as the initial point and going to step (b).

38. (Currently Amended) The method of claim 30, comprising the steps of:

- a) choose a starting point;
- b) initialization $j = 0$;
- c) applying a hybrid search method for Phase I using said starting point to find a feasible point in a (path-connected) feasible component, setting a point so found as an initial point, and applying the hybrid search method for Phase II to find a local optimal solution $x_{s,0}^j$;
- d) starting from said initial point $x_{s,0}^j$, applying a numerical method for Phase II to find all local optimal solutions in said feasible component and recording them as the set V_s^j and set $V_s = V_s \cup V_s^j$;
- e) for the local optimal solution $x_{s,0}^j$, defining a set of search vectors $S_i^j, i = 1, 2, \dots, k_j$;
- f) if $i > k_j$, then going to step (l), otherwise, going to step (g);

- g) for each search vector S_i^j , applying a reverse-time trajectory method to find a point lying in an unstable equilibrium manifold of a system (4.9), and if a point is found, letting it be denoted as $x_{d,j}^i$ and going to step (h), otherwise setting $i = i + 1$ and going to step (f);
- h) setting $x_{0,j}^i = x_s^j + (i + \varepsilon)(x_{d,j}^i - x_s^j)$, where ε is a small number and x_s^j is a local optimal solution selected in step (e), and applying the hybrid search method for Phase II using $x_{0,j}^i$ as the initial point to find a point lying in a stable equilibrium manifold of system (4.9) satisfying required conditions ~~(C1-1)~~ and ~~(C1-2)~~, and letting the solution be denoted as $x_{s,j}^0$;
- i) starting from said initial point $x_{s,j}^0$ and applying the hybrid search method of step (b) of claim 28 to find a local optimal solution in said (path-connected) feasible component $x_{s,0}^{j+1}$;
- j) checking whether $x_{s,0}^{j+1}$ has been found before, i.e. $x_{s,0}^{j+1} \in V_s$?, and if it has been bound before (i.e., the said feasible component has been visited before), then setting $i = i + 1$ and going to step (f), otherwise setting $V_s = V_s \cup \{x_{s,0}^j\}$ and $V_{new}^{j+1} = V_{new}^{j+1} \cup \{x_{s,0}^{j+1}\}$ and going to step (k);
- k) starting from said initial point $x_{s,0}^{j+1}$, applying a numerical method for Phase II to find all local optimal solutions in said feasible component and recording them in the set V_s^{j+1} , set $V_s = V_s \cup V_s^{j+1}$ and setting $i = i + 1$ and going to step (f);
- l) examining the set of all newly computed local optimal solutions V_{new}^{j+1} , and if V_{new}^{j+1} is empty, then going to the next step, otherwise, setting $j = j + 1$ and going to step (e); and

- m) identifying the global optimal solution from said set of local optimal solutions V_s by comparing their objective function values.

39. (Currently Amended) A numerical method for Phase II of claim 28, comprising the following steps to find all the local optimal solutions in said path-connected feasible component:

- a) given an initial point lying in said path-connected feasible component;
- b) initialization;
- c) applying a hybrid search method for Phase II using the initial point to find a local optimal solution x_s^0 , and setting $j = 0$, $V_s = \{x_s^0\}$, $V_{new,II}^j = \{x_s^0\}$ and $V_d = \{\emptyset\}$;
- d) for each local optimal solution in V_{new}^j (i.e., x_s^j), performing steps (e) through (k);
- e) defining a set of search vectors $S_i^j, i = 1, 2, \dots, m_j$, and setting $i = 1$;
- f) if $i > m_j$, then going to step (l), otherwise, applying a DDP search method, wherein a nonlinear dynamical system (4.10) satisfies required conditions (C2-1) and (C2-2) to find a corresponding dynamical decomposition point (DDP), and if a DDP is found, then going to step (g), otherwise, setting $i = i + 1$ and going to step (f);
- g) letting the found DDP be denoted as $x_{d,i}^j$, checking whether it belongs to the set V_d , i.e., $x_{d,i}^j \in V_d$?, and if it does, then setting $i = i + 1$ and going to step (f), otherwise setting $V_d = V_d \cup \{x_{d,i}^j\}$ and going to step (h);
- h) for the DDP $x_{d,i}^j$, performing steps (i) through (j) to find a corresponding adjacent local optimal solution;

- i) setting $x_{0,i}^j = x_s^j + (1 + \varepsilon)(x_{d,i}^j - x_s^j)$, where ε is a small number;
 - j) applying a hybrid search method using $x_{0,i}^j$ as the initial condition to find the corresponding local optimal solution, and letting it be denoted as $x_{s,j}^j$;
 - k) checking whether $x_{s,j}^j$ has been found before, i.e. $x_{s,j}^j \in V_s$?, and if it has already been found, then setting $i = i + 1$ and going to step (f), otherwise, setting $V_s = V_s \cup \{x_{s,j}^j\}$ and $V_{new}^{j+1} = V_{new}^{j+1} \cup \{x_{s,j}^j\}$ and setting $i = i + 1$ and going to step (f); and
 - l) examining the set of all newly computed local optimal solutions $V_{new,II}^{j+1}$, and if $V_{new,II}^{j+1}$ is non-empty, then setting $j = j + 1$ and proceeding to step (d), otherwise outputting all the local optimal solutions in said path-connected feasible component contained in set V_s and stopping the process.
40. (Previously Presented) A computer-implemented method for obtaining the global optimal solution of constrained nonlinear programming problems, comprising the steps of:
- a) using a transformation technique to transform a constrained optimization problem into an unconstrained optimization problem, then applying the following steps to find the global optimal solution of the unconstrained optimization problem;
 - b) choosing a starting point;
 - c) apply a hybrid search method using said starting point to find a local optimal solution x_s^0 ;
 - d) setting $j = 0$, $V_s = \{x_s^0\}$, $V_{new}^j = \{x_s^0\}$ and $V_d = \{\emptyset\}$;
 - e) setting $V_{new}^{j+1} = \{\emptyset\}$ and for each local optimal solution in V_{new}^j (i.e., x_s^j), performing steps (e) through (k);

- f) defining a set of search vectors S_i^j , $i = 1, 2, \dots, m_j$, and setting $i = 1$;
- g) if $i > m_j$, then going to step (l), otherwise, applying the DDP search method of claim 15 along the search vector S_i^j to find a corresponding dynamical decomposition point (DDP), and if a DDP is found, then going to step (g), otherwise, setting $i = i + 1$ and going to step (f);
- h) letting the found DDP be denoted as $x_{d,i}^j$, checking whether it belongs to the set V_d , i.e., $x_{d,i}^j \in V_d$?, and if it does, then setting $i = i + 1$ and going to step (f), otherwise setting $V_d = V_d \cup \{x_{d,i}^j\}$ and going to step (h);
- i) for the DDP $x_{d,i}^j$, performing steps (i) through (j) to find a corresponding adjacent local optimal solution;
- j) setting $x_{0,i}^j = x_s^j + (1 + \varepsilon)(x_{d,i}^j - x_s^j)$, where ε is a small number;
- k) applying a hybrid search method using $x_{0,i}^j$ as the initial condition to find the corresponding local optimal solution, and letting it be denoted as $x_{s,j}^i$;
- l) checking whether $x_{s,j}^i$ has been found before, i.e. $x_{s,j}^i \in V_s$?, and if it has already been found, then setting $i = i + 1$ and going to step (f), otherwise, setting $V_s = V_s \cup \{x_{s,j}^i\}$ and $V_{new}^{j+1} = V_{new}^{j+1} \cup \{x_{s,j}^i\}$ and setting $i = i + 1$ and going to step (f);
- m) examining the set of all newly computed local optimal solutions, V_{new}^{j+1} , and if V_{new}^{j+1} is non-empty, then setting $j = j + 1$ and proceeding to step (d), otherwise proceeding to the next step; and

n) identifying the global optimal solution from said set of local optimal solutions V_s by comparing their corresponding objective function values in set V_s ;
and

o) displaying the global optimal solution.

41. (Cancelled)

REMARKS

Claims 15-21, 23, 25-26, 28-33, and 37-40 remain in this case, no claims being added or cancelled by this response.

Case Status

This amendment after allowance is provided in response to a telephone call from Examiner Phan on April 3, 2007.

On October 4, 2006, Applicant filed a timely reply to a final rejection, rewriting the claims to make them allowable as indicated in the office action. This case received an "Allowance Counted" status on October 12, 2006. Prior to the six-month date for reply to the office action, on December 4, 2006, Applicant's attorney spoke to Examiner's supervisor, and was assured that the response had been timely filed and had been entered, that the "Allowance Counted" status meant that the case would be allowed, but was now under Quality Review. Therefore, this amendment is denoted as an "Amendment after Allowance", this terminology being approved on the advice of the Examiner.

In the telephone call today, the Examiner indicated that the Quality Review had indicated that the claims needed to be revised under section 112, because they contained parenthetical references to equations (i.e. "(4.5)") and to conditions (i.e. "(C1)"), the parentheticals referring to items defined in the specification.

Description of Amendments

Applicant has amended the claims to remove the references to the equations.

In most cases, the equations were already verbally described in the claim, so that no amendment was necessary beyond deleting the parenthetical number - see, for example, claim 15(c), "... a nonlinear system (4.2) ...". In a few cases, where the claim might be unclear after deletion of the parenthetical number, the claim was amended to replace the number by the verbal description from earlier in the claim - see, for example, claim 28, where the beginning of step (a) recites "... of the constrained optimization problem (4.7): ..." and step (a)(iii) is amended to read: "... in (4.7) the constrained optimization problem, and ...".

Similarly, as requested by the Examiner, the parenthetical notations (Cx) in the phrase "conditions (C1) and (C2)" (and other conditions (C1-1), etc.) are replaced by "... required conditions ...". The phrase "required conditions" is found in the specification on page 5, line 23 - it will be understood that this phrase is meant to apply to all of the conditions (C1), etc, which are referred to elsewhere in the specification simply as "conditions".

The removal of the parentheticals required a few minor amendments for grammatical consistency, primarily adding "the" or "said" as required. No change to the claims was intended.

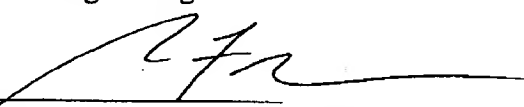
The amendments presented herein are purely for the clerical function of removing parenthetical references which were found unacceptable during the Quality Review and are not made in response to a rejection over prior art. No new matter is introduced, and no change to the scope of the claims is intended or should be implied.

Reconsideration of this case, as amended, is requested.

Conclusion

Applicant believes that all of the claims, as amended, are now patentable over the prior art, and that this case is now in condition for allowance of all claims therein. Such action is thus respectfully requested. If the Examiner disagrees, or believes for any other reason that direct contact with Applicants' attorney would advance the prosecution of the case to finality, he is invited to telephone the undersigned at the number given below.

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